

Problem #1 (P3): only a, d and g are true

Problem #2 (P6): $3.0 \times 10^{26} \text{ W} = 3.00 \times 10^{26} \frac{\text{J}}{\text{s}}$

$$E = \Delta mc^2$$

$$\Delta m = \frac{3 \times 10^{26} \frac{\text{J}}{\text{s}}}{\left(2.998 \times 10^8 \frac{\text{m}}{\text{s}}\right)^2} = \boxed{3.34 \times 10^9 \frac{\text{kg}}{\text{sec}}}$$

Problem #3 (P8): $\Delta t = 2 \mu\text{s} = 2 \times 10^{-6} \text{ s}$, $v = 0.6c$

$$\Delta t' = \Delta t \gamma = \frac{\Delta t}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{2 \times 10^{-6} \text{ s}}{\sqrt{1 - \left(\frac{0.6c}{c}\right)^2}}$$

$$\Delta t' = \frac{2 \times 10^{-6} \text{ s}}{\sqrt{1 - (0.6)^2}} = 2.5 \times 10^{-6} \text{ sec}$$

b) $\Delta x = v \Delta t = 0.6 (2.998 \times 10^8 \text{ m/s}) (2.5 \times 10^{-6} \text{ s}) =$

$$\Delta x = 449.7 \text{ m} = \boxed{0.4497 \text{ km}}$$

Problem #4(P17)

$L_p = 350 \text{ m}$

$v = 0.63c$

$t' = \text{Ship}, t = \text{tower}$

Pg #2

a) When is signal sent, according to nose of ship?
We may use the classical relation $t = \frac{L}{v} = \frac{350 \text{ m}}{0.76c} = 1.54 \times 10^{-6} \text{ s} = 1.54 \mu\text{s}$

b) When is signal received, according to nose of ship?
We will use the Inverse Lorentz time transformation

$$t' = \gamma(t - \frac{vx}{c^2}), \quad \gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = 1.54$$

$$t' = 1.54 \left(t_{\text{received}} - \frac{v(2.998 \times 10^8 \text{ m/s}) 350 \text{ m}}{(2.998 \times 10^8 \text{ m/s})^2} \right)$$

t_{received} is the proper time according to the nose: $t_{\text{sent}} + t_{\text{traverse}}$

$$t' = 1.54 (2.71 \times 10^{-6} - 0.887 \times 10^{-6})$$

$$t' = 2.81 \times 10^{-6} \text{ s} = 2.81 \mu\text{s}$$

$$\begin{aligned} t_{\text{received}} &= 1.54 \times 10^{-6} + \frac{L_p}{c} \\ t_{\text{received}} &= 1.54 \times 10^{-6} + \frac{350 \text{ m}}{2.998 \times 10^8 \text{ m/s}} \\ t_{\text{received}} &= 1.54 \times 10^{-6} + 1.17 \times 10^{-6} \\ t_{\text{received}} &= 2.71 \times 10^{-6} \text{ s} = 2.71 \mu\text{s} \end{aligned}$$

c) According to transmitter: $t_{\text{received}} = 2.81 \mu\text{s}$ from above

d) $x' = \gamma(x - vt) = 1.54(350 \text{ m} - 0.76c \cdot 2.81 \times 10^{-6} \text{ s}), \quad x' = -447 \text{ m}$

This Problem is very confusing - even when done in the Student Solution manual -
I disagree with several of the answers.

Problem #5 (P27): First use Kepler's 3rd Law to determine

$$T = 107 \text{ minutes} \\ = 6.42 \times 10^3 \text{ sec.}$$

radius: $T^2 = \frac{4\pi^2}{GM_E} r^3 \Rightarrow \frac{4\pi^2}{g_{RE}} r^3 \Rightarrow r = \sqrt[3]{\frac{g_{RE} T^2}{4\pi^2}}$

$$r = \sqrt[3]{\frac{(9.81 \text{ m/s}^2)(6370 \times 10^3 \text{ m})^2 (6.42 \times 10^3 \text{ s})^2}{4\pi^2}} = 7.46 \times 10^6 \text{ m}$$

Now determine v from: $v = \frac{2\pi r}{T}$ or $v^2 = \left(\frac{4\pi^2 r^2}{T^2}\right) = \frac{4\pi^2 (7.46 \times 10^6 \text{ m})^2}{(6.42 \times 10^3 \text{ s})^2} = 5.37 \times 10^7 \frac{\text{m}^2}{\text{s}^2}$

Now $\Delta t_0 = \frac{\Delta t'}{(1 - \frac{v^2}{c^2})}$ Since $v \ll c$ use Binomial Expansion

$$\Delta t_0 = \Delta t' \left(1 - \frac{v^2}{c^2}\right)^{-1/2} = \Delta t' \left(1 + \frac{1}{2} \left(\frac{v^2}{c^2}\right)\right)$$

Now $\Delta t = \Delta t' - \Delta t_0 = \Delta t' - \Delta t' \left(1 + \frac{1}{2} \frac{v^2}{c^2}\right) = \Delta t' \left(1 - \left(1 + \frac{1}{2} \frac{v^2}{c^2}\right)\right)$

$$\Delta t = \Delta t' \left(\frac{1}{2} \frac{v^2}{c^2}\right) = \Delta t' \left(\frac{1}{2}\right) \left[\frac{5.37 \times 10^7 \text{ m}^2/\text{s}^2}{(2.998 \times 10^8 \text{ m/s})^2}\right] = \Delta t' (2.99 \times 10^{-10})$$

$$\Delta t = (2.99 \times 10^{-10}) \left(\frac{31.56 \times 10^6 \text{ s}}{\text{yr}}\right) = 9.43 \times 10^{-3} \frac{\text{sec}}{\text{yr}} = 9.43 \frac{\text{m sec}}{\text{year}}$$

Problem #6 (P3A): Particle in frame S has $p = 7 \frac{MeV}{c}$ and total energy $E = 9 MeV$.

Pg #4

a). $E^2 = p^2 c^2 + E_0^2 \Rightarrow E_0^2 = E^2 - (pc)^2, E_0 = m_0 c^2$

$$E_0 = \sqrt{E^2 - p^2 c^2} = \sqrt{(9 MeV)^2 - (7 \frac{MeV}{c})^2 c^2} = \sqrt{(81 - 49) MeV^2} = 5.66 MeV$$

$$m_0 = \frac{E_0}{c^2} = \frac{5.66 \times 10^6 eV + 1.602 \times 10^{-19} J}{(2.998 \times 10^8 m/s)^2} = 1.008 \times 10^{-29} kg$$

b). $E^2 = p^2 c^2 + E_0^2, E_0 = 5.66 MeV$

$$E = \sqrt{(4 \frac{MeV}{c})^2 c^2 + (5.66 MeV)^2} = 6.93 MeV$$

c). To find relative speeds use Lorentz velocity trans:

$$u_b = \frac{u_a - v}{1 - \frac{v u_a}{c^2}}$$

$u_a \equiv$ Part a velocity
 $u_b \equiv$ Part b velocity

Solving for $v = \frac{u_a - u_b}{1 - \frac{u_a u_b}{c^2}}$

now need to determine $u_a \rightarrow u_b$:

$$E^2 = E_0^2 \gamma^2 = \frac{E_0^2}{1 - \frac{u^2}{c^2}} \Rightarrow \text{We can solve for } u = c \sqrt{1 - \left(\frac{E_0}{E}\right)^2}$$

$$u_a = c \sqrt{1 - \left(\frac{5.66 MeV}{9 MeV}\right)^2}$$

$$u_a = 2.33 \times 10^8 m/s$$

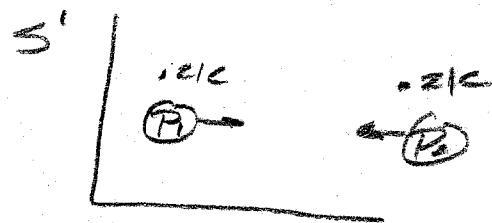
$$u_a = .777c$$

$$u_b = c \sqrt{1 - \left(\frac{5.66}{6.93}\right)^2}$$

$$u_b = 1.73 \times 10^8 m/s = .577c$$

$$v = \frac{.777c - .577c}{1 - (.777c)(.577c)} = .363c = 1.08 \times 10^8 \frac{m}{s}$$

Problem #7 (P37):



For any proton

Pg #5

$$K' = mc^2\gamma - mc^2 = E_0(\gamma - 1)$$

mc^2 for a proton: 938 MeV.

a) For one proton $K' = 938 \text{ MeV} \left(\sqrt{\frac{c^2}{c^2 - u^2}} - 1 \right) = 938 \text{ MeV} \sqrt{\frac{c^2}{c^2 - (0.21c)^2}} - 1$

$$K' = 21.4 \text{ MeV}$$

For both protons $K'_{\text{total}} = 42.8 \text{ MeV}$.

b) Let one proton be moving in frame S, $K' = (\gamma - 1) E_0$. S is moving at same speed as proton. Find velocity of proton in frame S: $u = \frac{u_1 + v}{1 + \frac{v u_1}{c^2}} = \frac{0.21c + 0.21c}{1 + \frac{(0.21c)(0.21c)}{c^2}} = 0.402c$

γ in moving frame is: $\frac{1}{\sqrt{1 - \frac{u^2}{c^2}}} = \frac{1}{\sqrt{1 - \frac{(0.402c)^2}{c^2}}} = 1.09$

$$K = (1.09 - 1) 42.8 \text{ MeV} = 3.94 \text{ MeV}$$

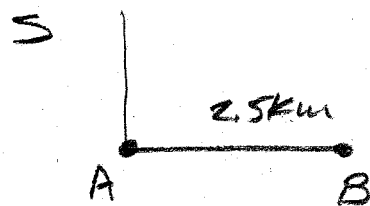
Problem # 8 (P2):

Due to gravitational time dilation > Stronger $g \Rightarrow$ Slower time

Pg #6

Thus, twin working in basement will age slower.

Problem # 9 (P10):



$$\Delta t_{BA} = 2 \times 10^{-6} \text{ s.}$$

using Lorentz time transform:

a)

$$\Delta t' = t'_B - t'_A = \gamma \left[(t_B - t_A) - \frac{v}{c^2} (x_B - x_A) \right]$$

$$\Delta t' = \gamma \left(\Delta t - \frac{v}{c^2} \Delta x \right)$$

we wish to find v such that $\Delta t' = 0$

$$\gamma \left(\Delta t - \frac{v}{c^2} \Delta x \right) = 0 \Rightarrow \gamma \Delta t - \frac{\gamma v}{c^2} \Delta x = 0$$

$$\gamma \Delta t = \frac{\gamma v}{c^2} \Delta x \Rightarrow \gamma v = \frac{\gamma \Delta t c^2}{\Delta x} \Rightarrow v = \frac{\Delta t c^2}{\Delta x}$$

$$v = \left(\frac{(2 \times 10^{-6} \text{ s}) c}{2.5 \times 10^3 \text{ m}} \right) c = .24c$$

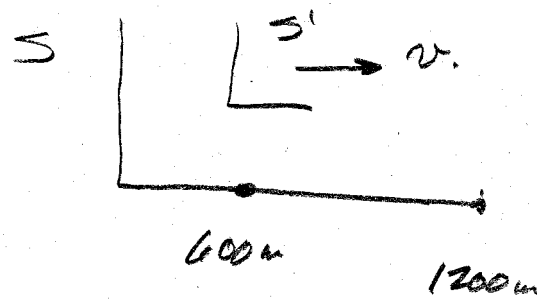
b) for B to occur before A, $\Delta t < 0$

$$\Delta t' = \gamma \left(\Delta t - \frac{v \Delta x}{c^2} \right) < 0 \Rightarrow \Delta t < \frac{v \Delta x}{c^2} ; v > \frac{\Delta t c^2}{\Delta x}$$

$$v > .24c$$

Thus if $v > .24c$, event B will be seen before event A for the observer moving $> 0.24c$.

Problem #10(P19):



$$\Delta t = 6 \mu s$$

$$\text{for } S' \quad \Delta x' = 0$$

Determine $\Delta t'$

first determine v from $\Delta x' = \gamma(\Delta x - v\Delta t)$, $\Delta x' = 0$

$$\Delta x = v\Delta t \Rightarrow v = \frac{\Delta x}{\Delta t} = \frac{600 \text{ m}}{6 \times 10^{-6} \text{ s}} = 100 \times 10^6 \text{ m/s}$$
$$= 1 \times 10^8 \text{ m/s} = .334c.$$

$$\text{now } \Delta t' = \gamma\left(\Delta t - \frac{v\Delta x}{c^2}\right); \quad \gamma = \frac{1}{\sqrt{1 - .334^2}} = 1.06$$

$$\Delta t' = 1.06 \left[6 \times 10^{-6} \text{ s} - \frac{600 \text{ m} (.334c)}{c^2} \right] = 5.45 \times 10^{-6} \text{ s} = 5.45 \mu s.$$

Pg#7