

Ex: For $\theta = 5^\circ$, $\theta = 0.08727 \text{ rad}$

so $\theta = 0.08727 \text{ rad}$

$$\sin \theta = 0.08716$$

so $\sin \theta \sim \theta$ is good to $\sim 0.1\%$

For $\theta = 20^\circ$, $\theta = 0.3491 \text{ rad}$

so $\theta = 0.3491 \text{ rad}$

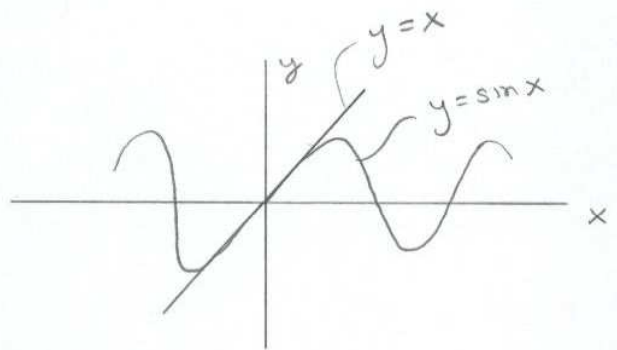
$$\sin \theta = 0.3420$$

so $\sin \theta \sim \theta$ is good to $\sim 2\%$

$\theta = 45^\circ$, $\sin \theta \sim \theta \sim 11\%$.

Recall: $y = \sin x$

$$\frac{1}{x} \quad y = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$$



∴ for small oscillations ($\theta \ll 1 \text{ rad}$) $\sin \theta \approx \theta$!

$$\frac{d^2 \theta}{dt^2} = -\omega^2 \sin \theta \quad \text{becomes} \quad \frac{d^2 \theta}{dt^2} = -\omega^2 \theta \quad \underline{\underline{\text{SHM!}}}$$